

Momentum Equations:

$$\frac{\partial u}{\partial t} - \frac{uv \tan \phi}{a} + \frac{uv}{a} = -\frac{1}{f a \cos \phi} \frac{\partial p}{\partial \lambda} - 2Q v \sin \phi$$

Cor.

$\frac{\partial u}{\partial t}$ mat. derivative
 $\frac{\partial}{\partial \lambda}$ metric term
 $\frac{\partial p}{\partial \lambda}$ metric term

$\frac{\partial p}{\partial \lambda}$ PGF
 $-2Q v \sin \phi$
 $+ 2Q w \cos \phi$
 $+ f_{rx}$

$\frac{\partial u}{\partial t}$ Nontrad. Coriolis
 f_{rx} molecular friction

$$\frac{\partial u}{\partial t} = u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z} + \frac{\partial u}{\partial t}$$

$$\frac{U}{T} = \frac{10 \text{ ms}^{-1}}{10^5 \text{ s}} = 10^{-4} \text{ ms}^{-2}$$

Mat. Der

$$\frac{U^2}{Q^2} = \frac{10^2}{10^7} = 10^{-5} \text{ ms}^{-1}$$

Metric term

$$2Q \sin \phi v = 10^{-4} \text{ ms}^{-1}$$

Cor

$$2Q \cos \phi w = \text{Need to use mass cont.}$$

$$\nabla \cdot \vec{v} = \frac{1}{g} \frac{\partial \rho w}{\partial z} \rightarrow \frac{U}{L} = \frac{w}{H}$$

height

$$w = \frac{U H}{L}$$

length

$$2Q \cos \phi w = 10^{-4} 10^0 10^{-1} = 10^{-5}$$

Nontrad. Coriolis

 $= \frac{10^1 10^4}{10^6} = 10^{-1} \text{ ms}^{-1}$

The tropical thermodynamic equation

In p-coords:

$$C_p \frac{\partial T}{\partial t} - \alpha \omega = Q$$

$\alpha = \frac{1}{g}$
 diabatic heating

 $\omega = \frac{\partial p}{\partial t}$

We also have hydrostatic balance

$$\frac{\partial \bar{p}}{\partial p} = -\alpha$$

Replace α in thermo budget:

$$C_p \frac{\partial T}{\partial t} + \omega \frac{\partial \Phi}{\partial P} = Q$$

"work"

$$C_p \frac{\partial T}{\partial t} + \vec{v} \cdot \nabla_h C_p T + \omega \left(\frac{\partial C_p T}{\partial P} + \frac{\partial \Phi}{\partial P} \right) = Q$$

$$DSE = C_p T + \Phi \quad \text{"dry static energy"}$$

$$C_p \frac{\partial T}{\partial t} + \vec{v} \cdot \nabla_h C_p T + \omega \frac{\partial DSE}{\partial P} = Q \quad \begin{matrix} \text{tropical} \\ \text{thermo egn. !} \end{matrix}$$

Eq. (1)

Many scientists assume that Φ is hor. and temporally homogeneous, i.e. $\Phi = \Phi(P)$. As a result, we add it to Eq. (1) to obtain:

$$\frac{\partial DSE}{\partial t} \approx Q \quad DSE \text{ budget}$$